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**JAN DE BEULE**, Vrije Universiteit Brussel

*A lower bound on the size of linear sets on a projective line of finite order*

A set  $S$  of points of the finite projective space  $\text{PG}(\mathbb{F}_q^{n+1})$  is a *linear set* of rank  $t$  if  $S = \{\langle u \rangle_F \mid u \in U\}$  for some set  $U \subset \mathbb{F}_q^{n+1}$  that is a  $t$ -dimensional vector space over a subfield of  $\mathbb{F}_q$ .

The following result was obtained jointly with Geertrui Van de Voorde: *An  $\mathbb{F}_q$ -linear set of rank  $k \leq n$  in  $\text{PG}(1, q^n)$  which contains at least one point of weight one, contains at least  $q^{k-1} + 1$  points.*

This result, its connection with direction problems in affine spaces, and some applications will be discussed.