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## Graphs and Games: the Mathematics of Richard Nowakowski (Part III)

(Org: Nancy Clarke (Acadia University))

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**ART FINBOW**, Saint Mary's University

*Extendable Vertices in Well-Covered Graphs*

A graph  $G$  is said to be *well-covered* if every maximal independent set of vertices in  $G$  has the same cardinality. A vertex  $v$  in a well-covered graph  $G$  is said to be *extendable* provided both (1)  $G \setminus v$  is well-covered and (2) the independence numbers of  $G$  and  $G \setminus v$  are equal. We present both a survey of results regarding such vertices and some extensions of this idea.

This work is joint with various sets of coauthors, the union of which includes **R. Nowakowski**, B. Hartnell, M. D. Plummer and C. Whitehead.

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**BERT HARTNELL**, Saint Mary's University

*Parity Dissociation Graphs*

Finding the dissociation number of an arbitrary graph (the cardinality of the largest set of vertices in an induced subgraph of maximum degree one) is difficult. If one is given a graph in which every maximal such set of vertices is maximum (in the spirit of well-covered graphs) then it is straight forward. Recent work has characterized graphs with this property that have girth 7 or more. Here we illustrate attempts to tighten the girth restriction as well as looking at a broader collection, those graphs in which every maximal dissociation set is of the same parity.

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**JEANNETTE JANSSEN**, Dalhousie University

*An application of Hall's theorem to linear embeddings of graphs*

Given a graph of order  $n$ , and any set of  $n$  locations on the real line, what is the best embedding of the vertices of  $G$  into these locations, so that the sum of squares of the distances of adjacent vertices is minimized? If the graph in question has a clear linear structure, i.e. is a proper interval graph, does the optimal embedding follows the natural ordering of the vertices? We give an affirmative answer for a special class of interval graphs, where the proof involves an application of Hall's theorem. Joint work with Nauzer Kalyaniwalla and Islay Wright.