

The Zero-Voltage Conductance of Nano-Graphenes: Simple Rules and Quantitative Estimates

Mayou, Zhou, Ernzerhof,
J. Phys. Chem. C, **2013**,
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Acknowledgments

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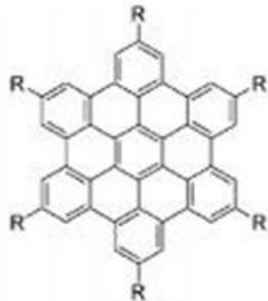
- Didier Mayou, Néel Institute, Grenoble*
- Martin Kaupp, Hilke Bahmann Technische, Universität Berlin*
- Michel Coté, UofM*

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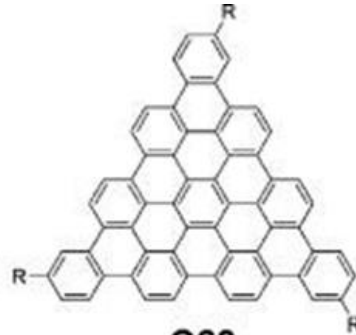


Polycyclic aromatic hydrocarbons (PAH), nowadays nano-graphene

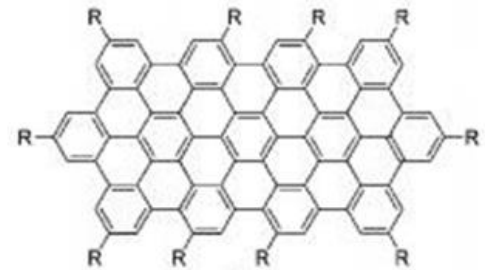
Kekulé molecules:



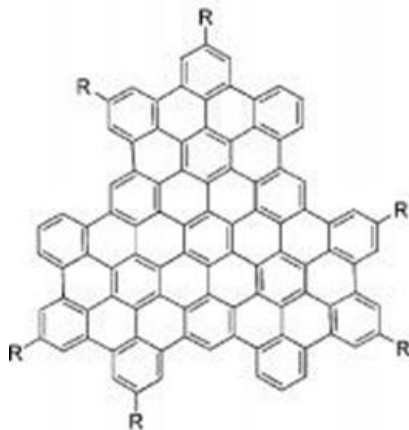
C42



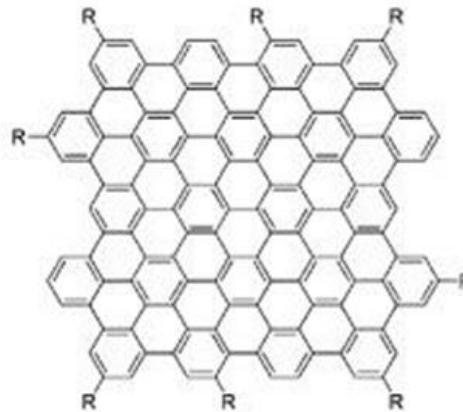
C60



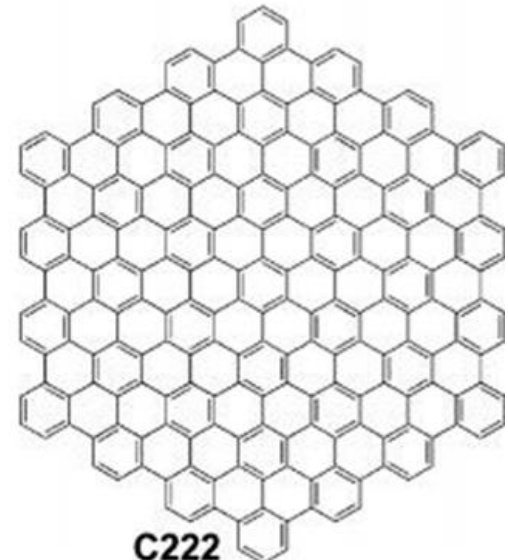
C78



C96



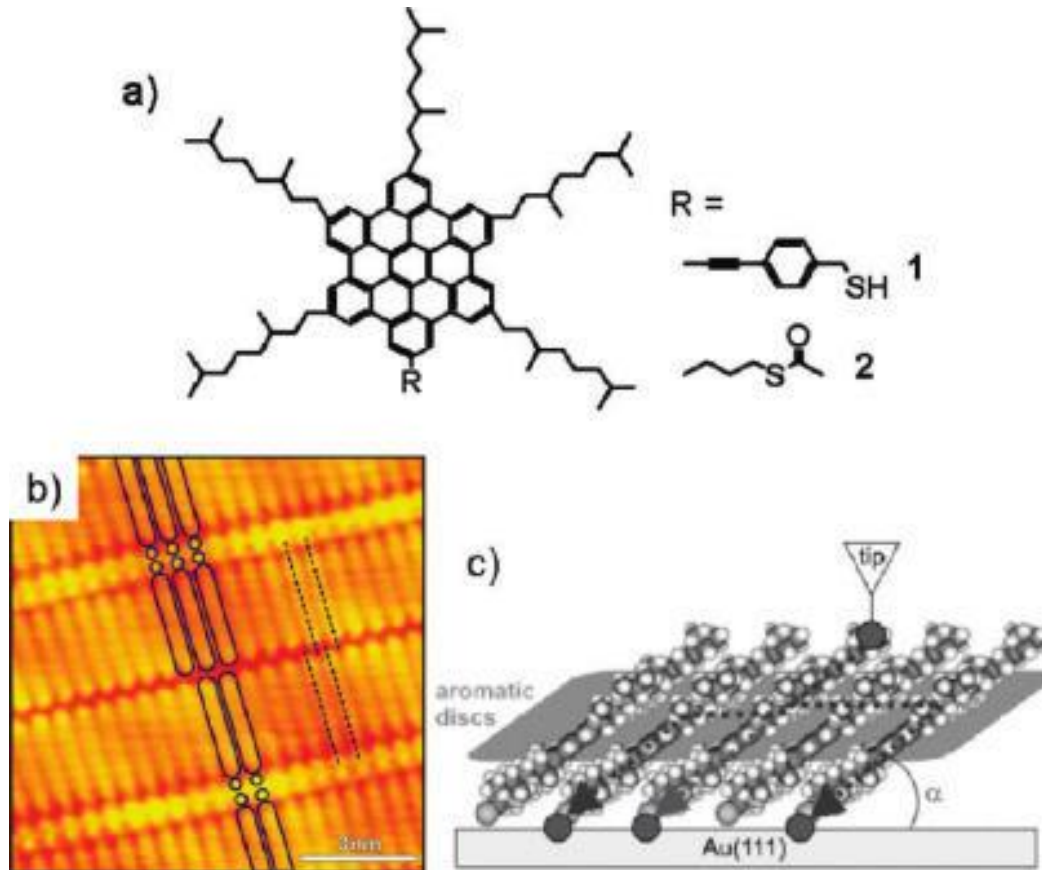
C132



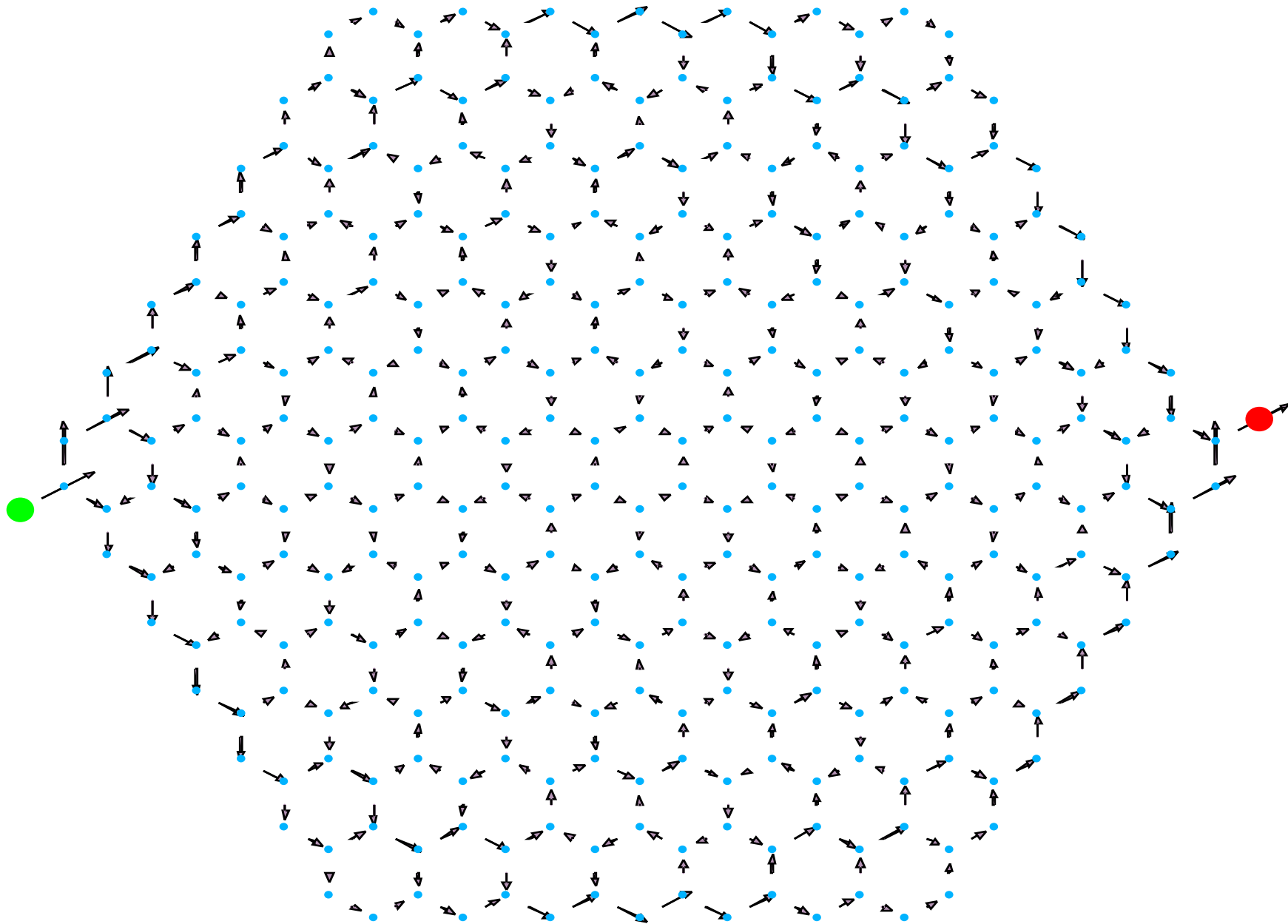
C222

Müllen group, Max Planck Institut, Mainz

Molecular electronics

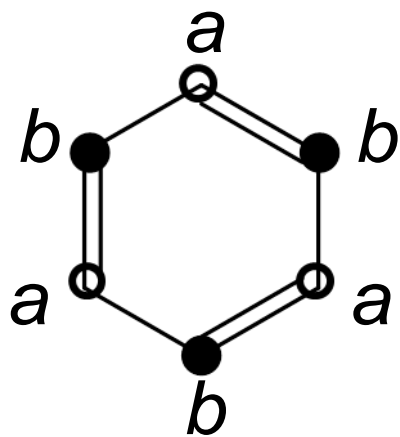
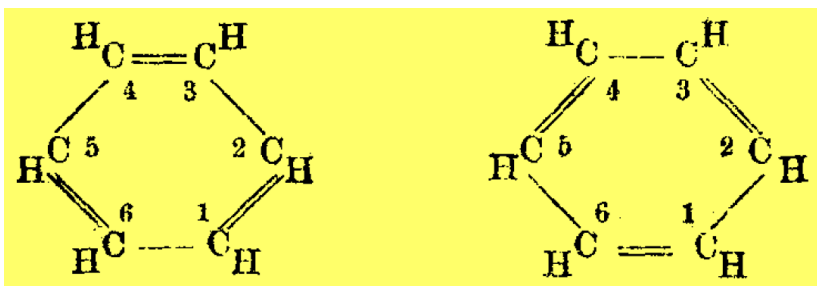


Käfer, Bashir, Dou, Witte, Müllen, Wöll,
C. Adv. Mater. 2010, 22, 384.



Separation of Kekulé molecules into two types of carbons

*Friedrich August
Kekulé von Stradonitz
(1829-1896).*

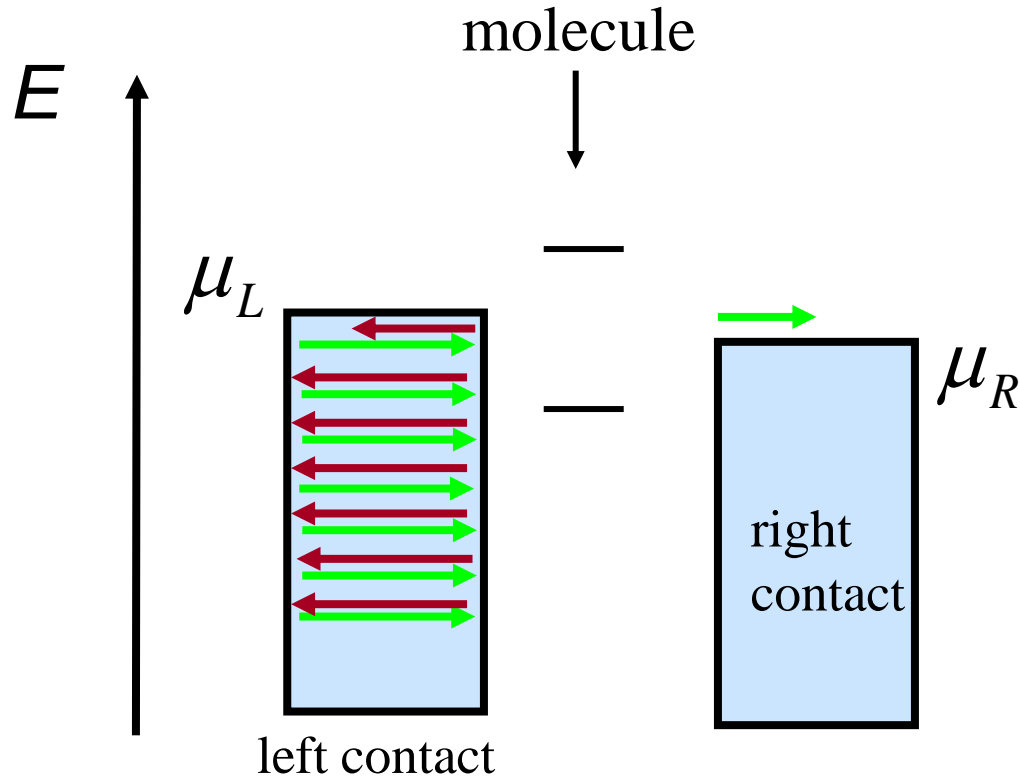


bipartite



*Chemisches Institut,
Universität Bonn*

Landauer formula

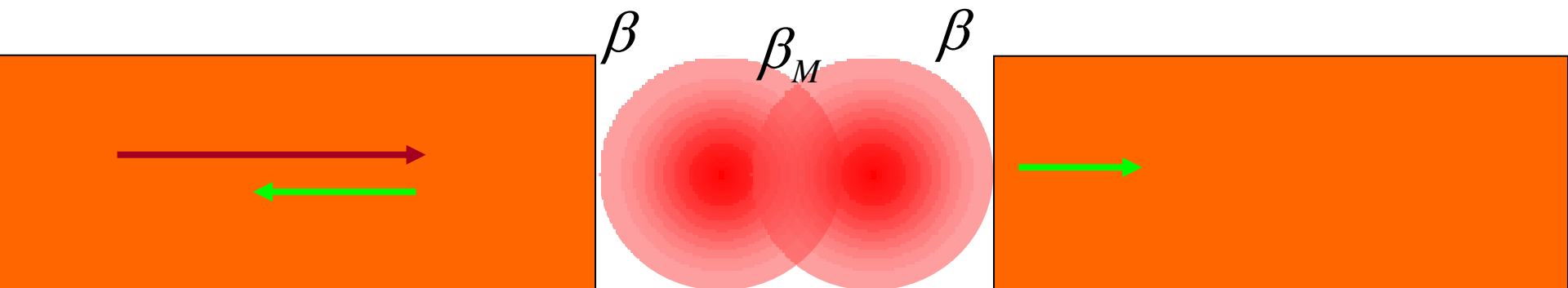


$$\Psi_L = \varphi^+ + r\varphi^- \quad \Psi_R = t\varphi^+$$

$$T(E) = |t(E)|^2 = 1 - |r(E)|^2$$

$$g(E) = \frac{e^2}{h} T(E)$$

The source-sink potential approach in tight binding (Hückel)



$$H^{\text{eff}}(r) = \begin{pmatrix} \Theta_L(r) & \beta_M \\ \beta_M & \Theta_R \end{pmatrix}$$

$$\Theta_L(r) = -i\beta \frac{1+r}{1-r}$$

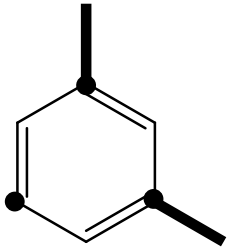
$$\Theta_R = i\beta$$

Goyer, Ernzerhof, Zhuang,
JCP, 126,144104 (2007):
Ernzerhof, JCP 126,144104
(2007).

Source and sink potential

Simple theory for the conductance of conjugated systems (aa case)

Contacts connected to two a atoms



$$H = \begin{pmatrix} H_{AA} & M_{AB} \\ M_{BA} & H_{BB} \end{pmatrix}$$

Reference energy of the atoms is set to 0

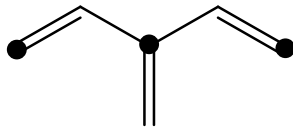
$$H_A^{\text{eff}} = H_{AA} + \Theta_L(r) + \Theta_R - M_{AB} \frac{1}{H_{BB} - E} M_{BA}$$

$\rightarrow \infty \Rightarrow$ no transmission

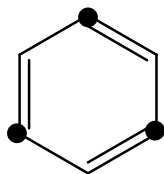
Simple theory for the conductance of conjugated systems (aa case)

Contacts connected to two a atoms

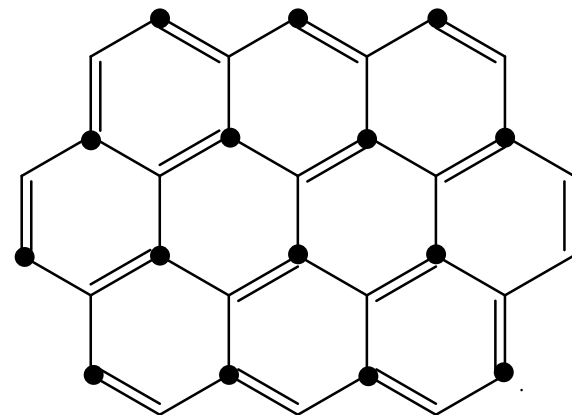
Cross-conjugation



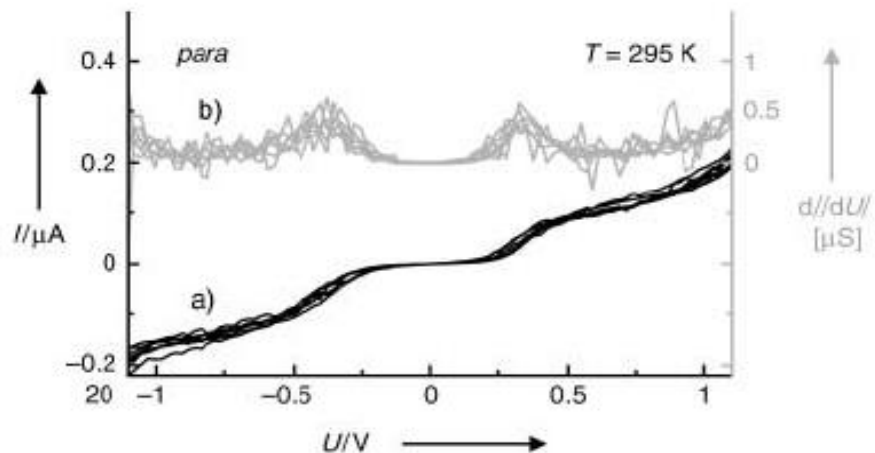
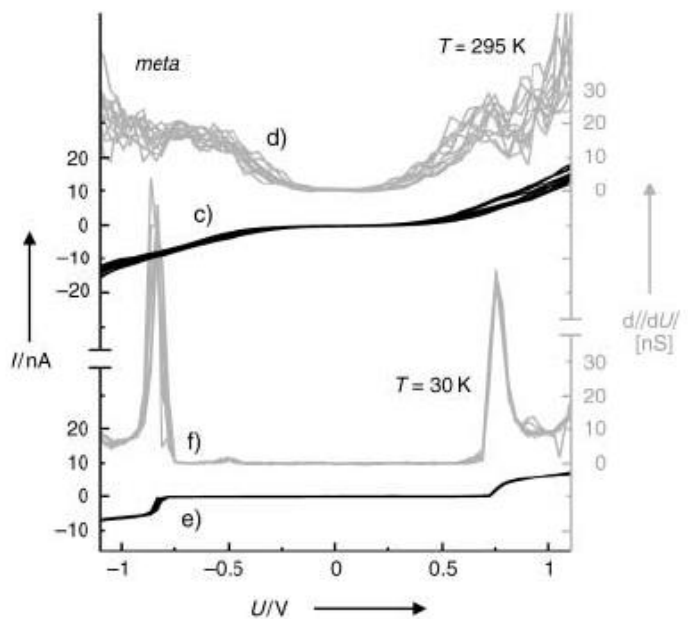
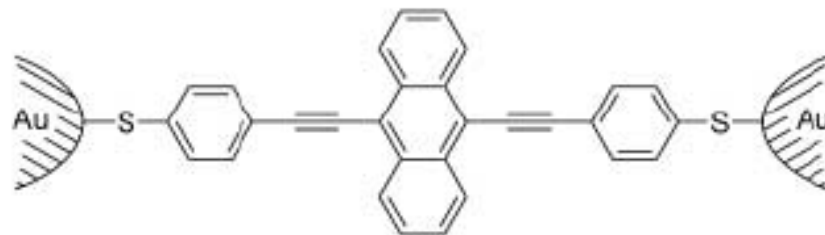
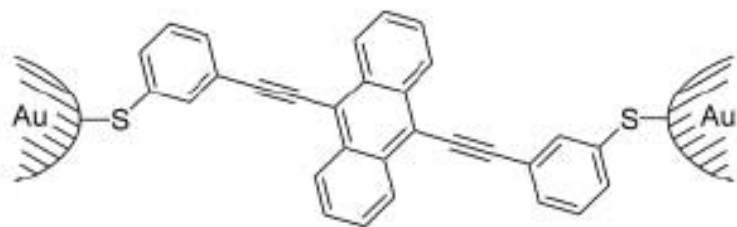
Meta vs. ortho & para connection



PAH



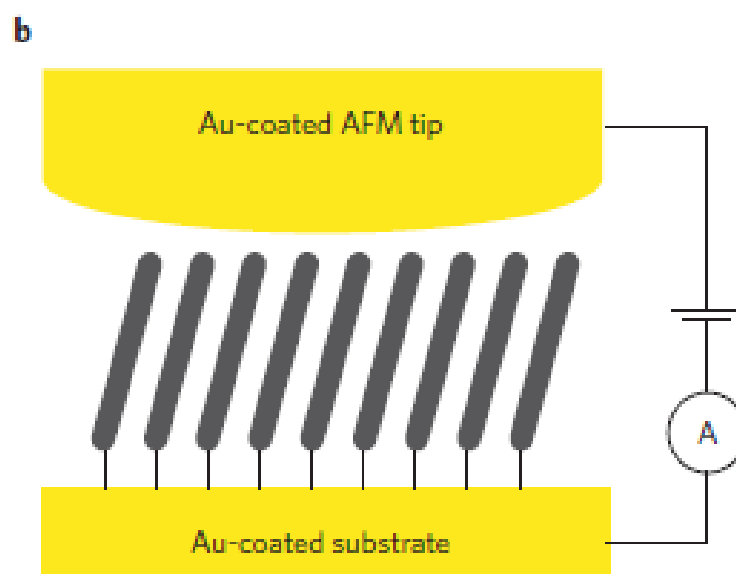
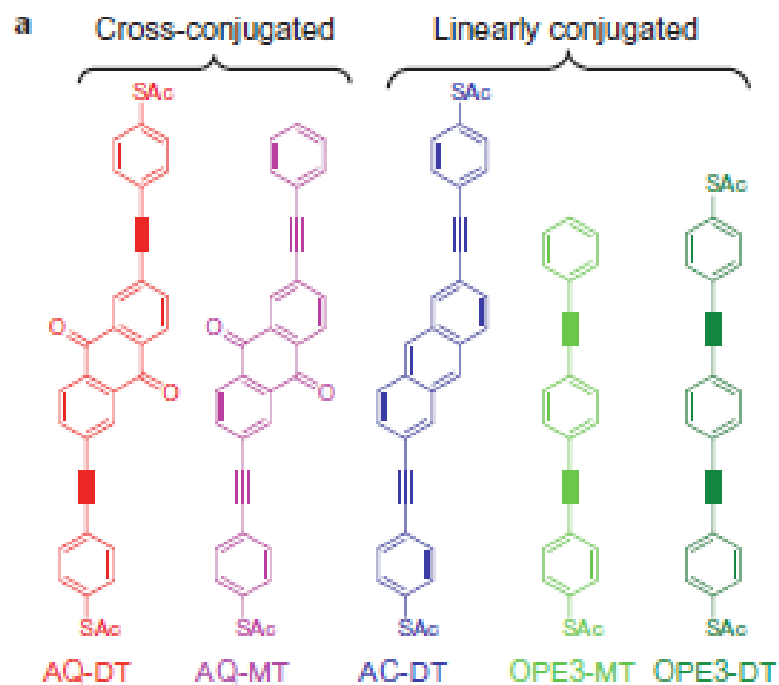
Impact of the position of the anchor group on molecular conductance



Mayor, Weber, Reichert, Elbing, von Hänisch, Beckmann, Fischer, Ang. Chemie Int. Ed., 42, 5834-5838 (2003)

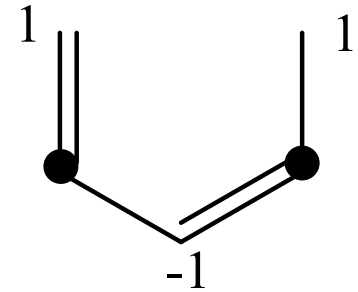
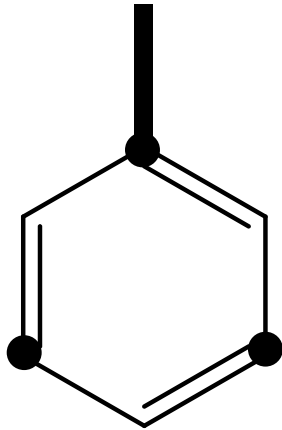
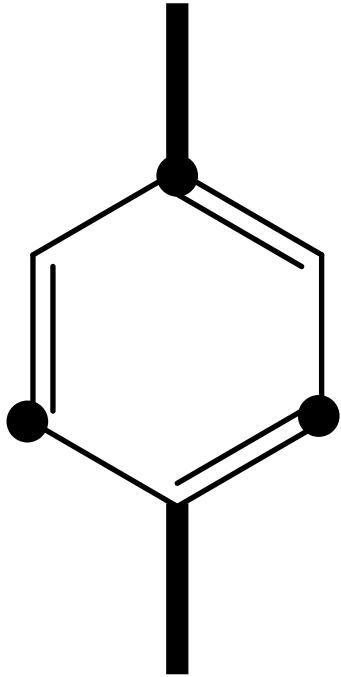
Observation of quantum interference in molecular charge transport

Constant M. Guédon^{1†}, Hennie Valkenier^{2†}, Troels Markussen³, Kristian S. Thygesen³,
Jan C. Hummelen² and Sense Jan van der Molen^{1*}



Ernzerhof, Zhuang, Rocheleau,
JCP 123, 134704, (2005)

Simple theory for the conductance of conjugated systems (ab case)



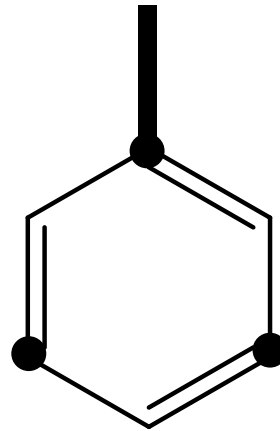
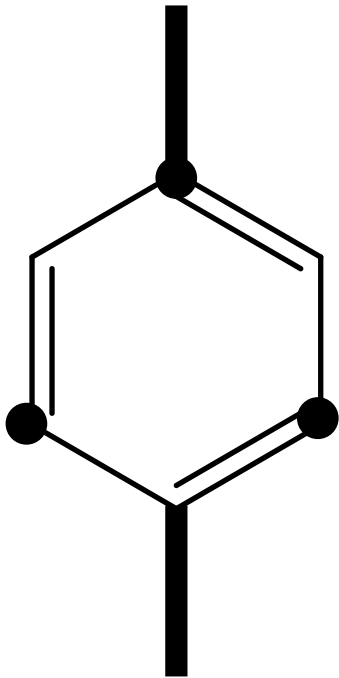
Longuet-Higgins, *J. Chem. Phys.* 1950, 18, 265.

$$\mathbf{H}_{Ab}^{\text{eff}} = \mathbf{H}_{AA} + \mathbf{h}_{bb} + \Theta_L^b(r) + \Theta_R^a + \mathbf{M}_{Ab} + \mathbf{M}_{bA} - \mathbf{M}_{ACb} \frac{1}{\mathbf{H}_{CbCb}} \mathbf{M}_{CbA}$$

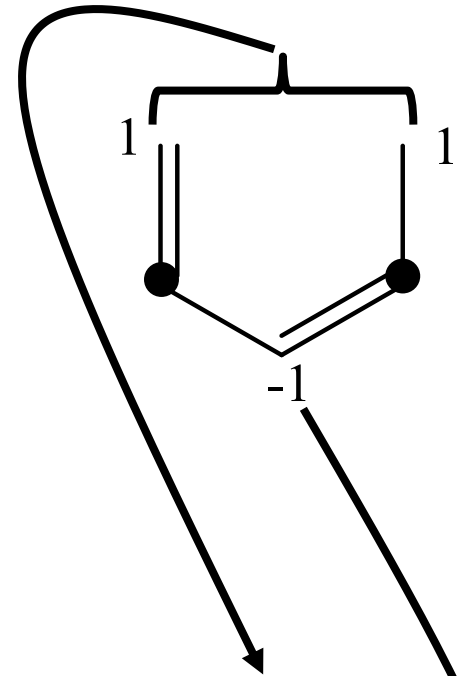
$$\mathbf{H}_{Ab}^{\text{eff}} = \begin{pmatrix} |c_a|^2 \Theta_L(r) & t \sum_{l \in ad(b)} c_l \\ t \sum_{l \in ad(b)} c_l & \Theta_R \end{pmatrix}$$

Simple theory for the conductance of conjugated systems (ab case)

*Contacts connected to an **a** and a **b** atom*



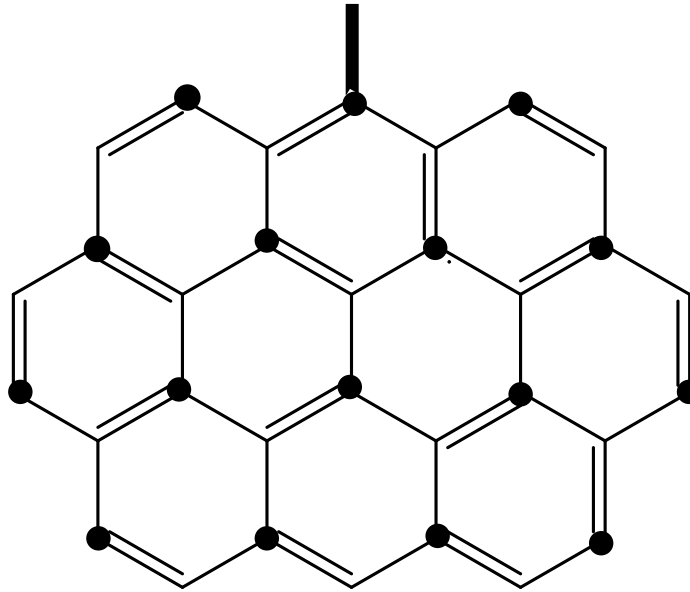
Defect state



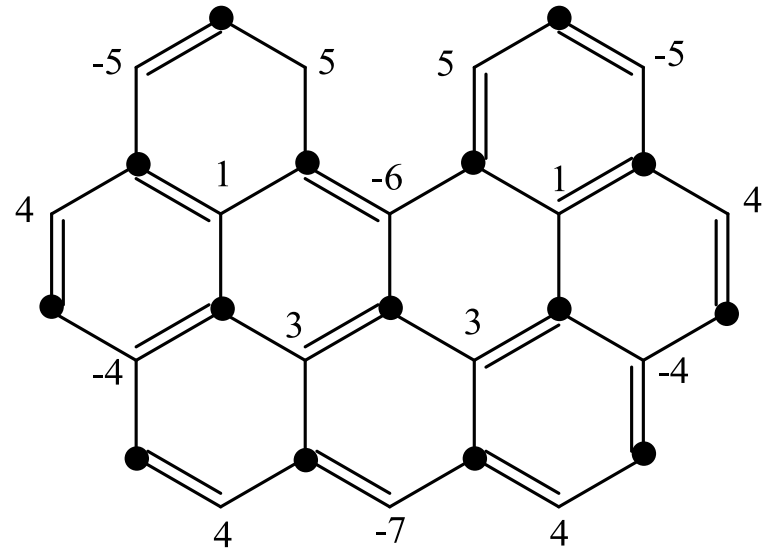
$$T(E = 0) = 4s / (1 + s)^2$$

$$s = \frac{t^2 \left(\sum_{l \in \text{ad}(b)} c_l \right)^2}{\beta^2 |c_a|^2}$$

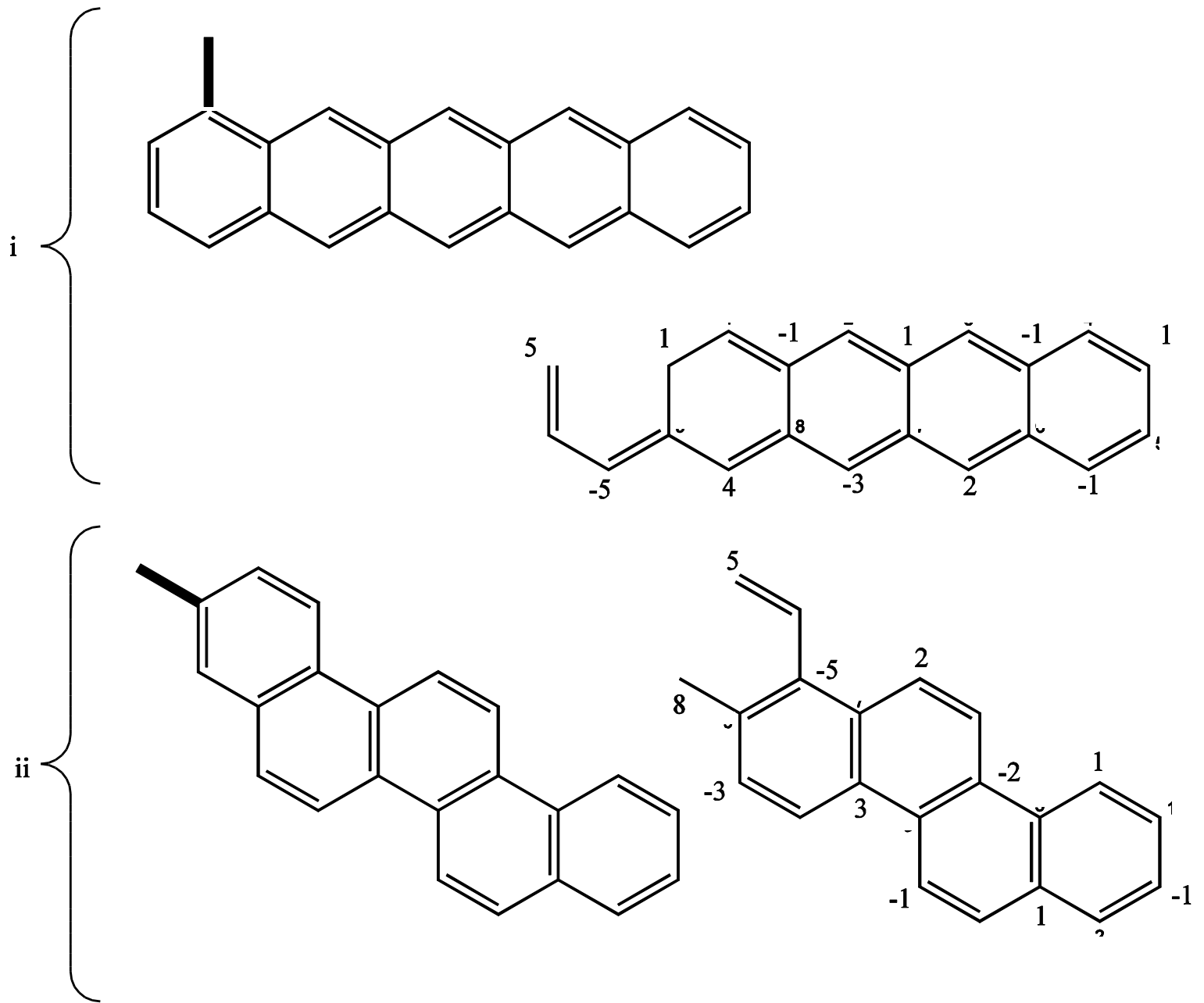
Ovalene



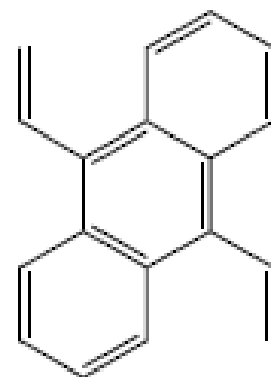
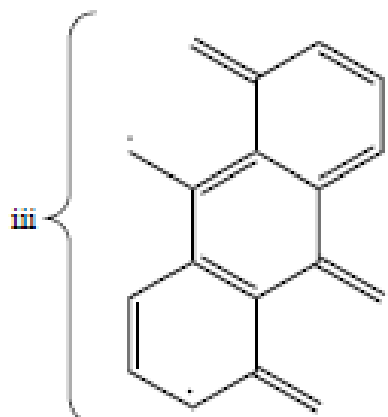
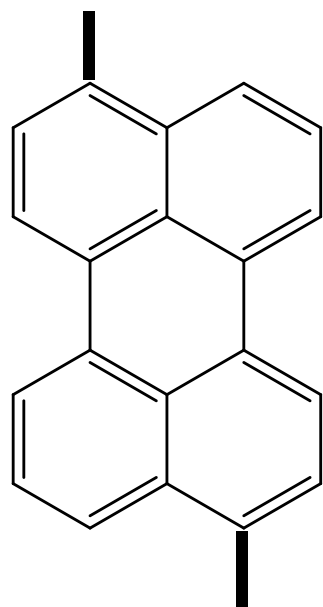
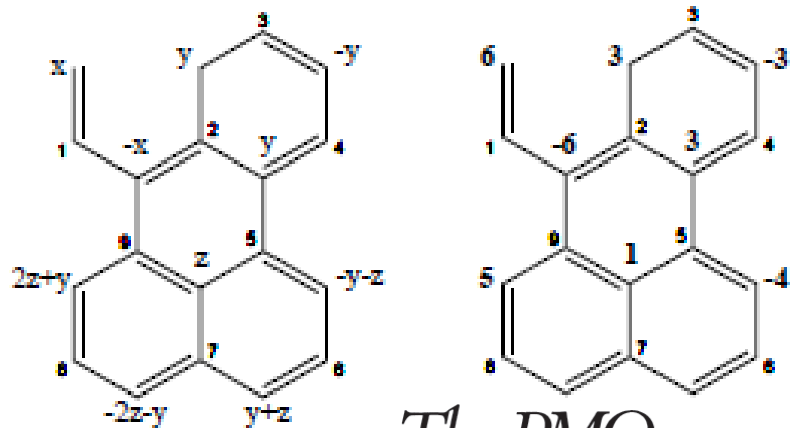
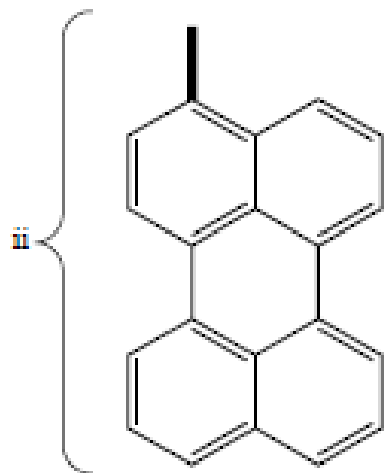
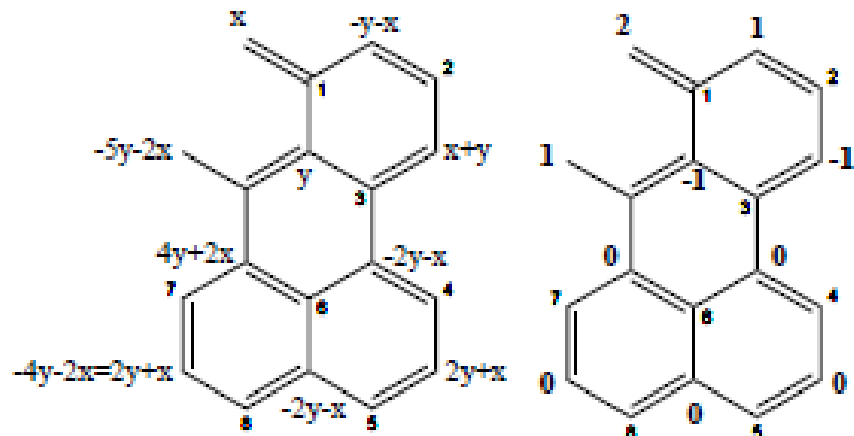
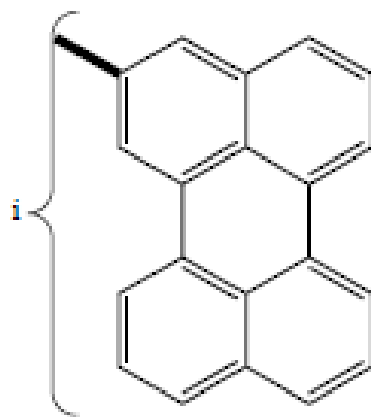
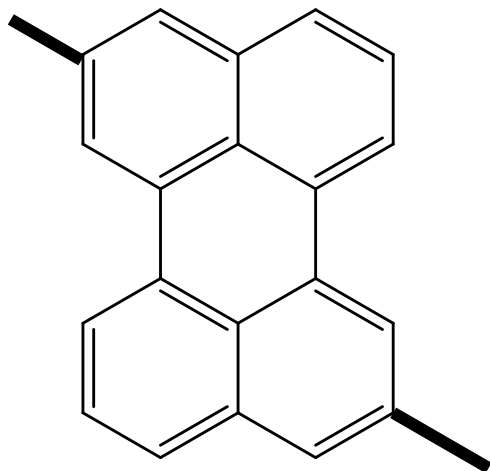
Delocalized defect state



Pentacene & Picene



Perylene



*The PMO
Theory of
Organic Chemistry*

Michael J. S. Dewar

Department of Chemistry
University of Texas
Austin, Texas

and

Ralph C. Dougherty

Conductance in terms of Kekulé structures

THE JOURNAL OF CHEMICAL PHYSICS 131, 244110 (2009)

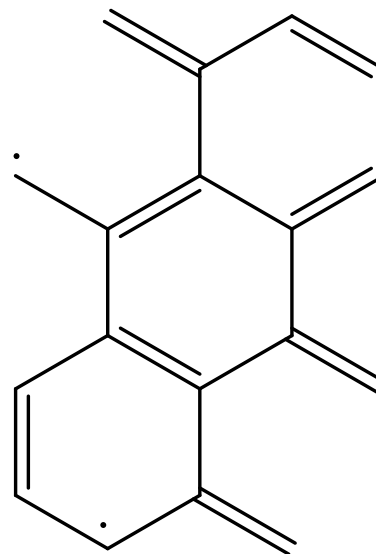
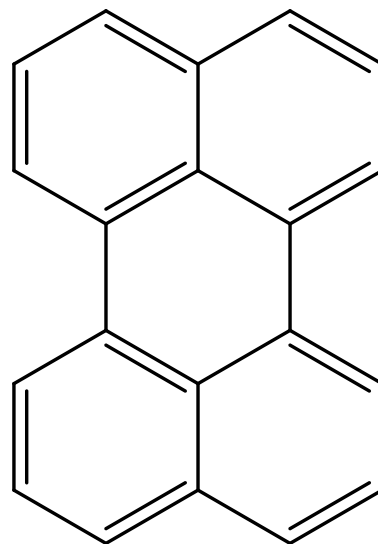
Conduction in graphenes

P. W. Fowler,^{1,a)} B. T. Pickup,^{1,b)} T. Z. Todorova,^{1,c)} and W. Myrvold^{2,d)}

¹Department of Chemistry, The University of Sheffield, England S3 7HF, United Kingdom

²Department of Computer Science, University of Victoria, British Columbia V8W 3P6, Canada

$$T(0) = \frac{4K_s^2 K_v^2 \bar{\beta}^2}{(K_s^2 + K_v^2 \bar{\beta}^2)^2}$$



Fowler, Pickup, Todorova, Myrvold, JCP, 131, 244110 (2009).

All electron DFT/Green's function approach

